

Curious about Data Science? Learn how it's applied in different jobs!







Assessing Continuous Data: Normal Distribution

Dr. Ab Mosca (they/them)

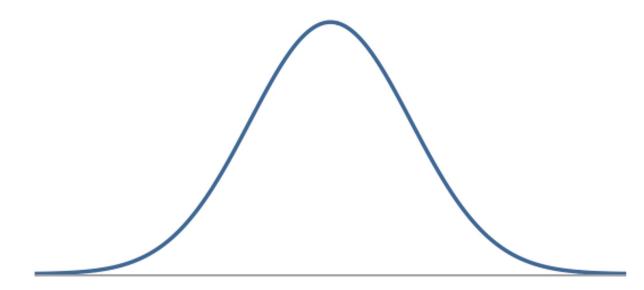
Slides based off slides courtesy of OpenIntro and John McGreedy of Johns Hopkins University

Plan for Today

- Shape of normal distributions
- Z Scores
- Percentiles
- Cutoff points

Normal Distribution

- Unimodal and symmetric, bell shaped curve
- Many variables are nearly normal, but none are exactly normal
- Denoted as $N(\mu, \sigma) \rightarrow$ Normal with mean μ and standard deviation σ



Normal distributions with different parameters

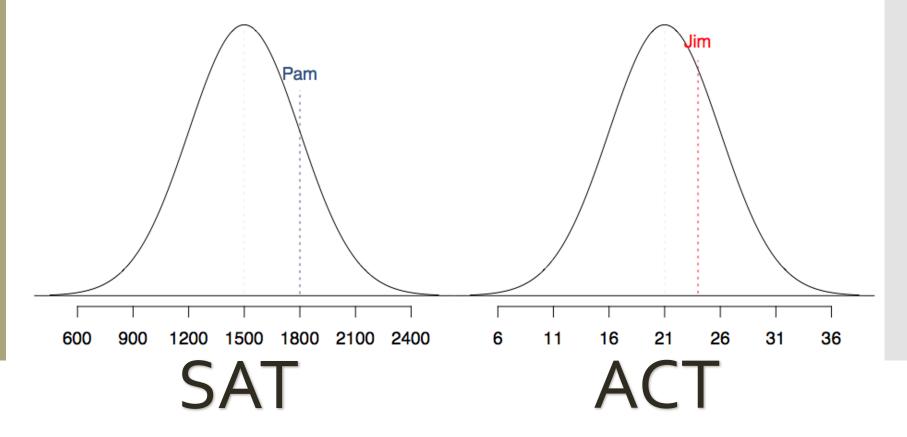
 μ : mean, σ : standard deviation

 $N(\mu = 0, \sigma = 1)$ $N(\mu = 19, \sigma = 4)$ -3 -2 -1 2 7 11 15 19 23 27 31 0 3 1 10 20 30 0

Practice

Find a group. Draw the following normal distributions on the board: *a)* $N(\mu = 0, \sigma = 10)$ *b)* $N(\mu = 10, \sigma = 5)$ *c)* $N(\mu = 85, \sigma = 2)$

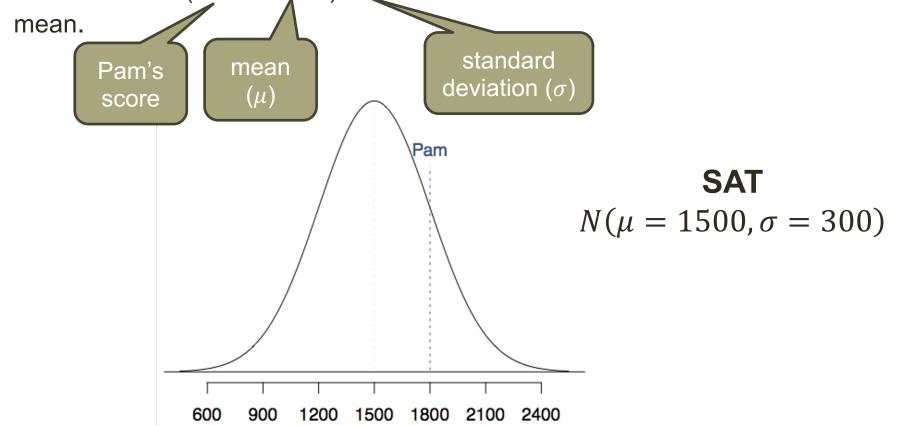
SAT scores are distributed nearly normally with mean 1500 and standard deviation 300. ACT scores are distributed nearly normally with mean 21 and standard deviation 5. A college admissions officer wants to determine which of the two applicants scored better on their standardized test with respect to the other test takers: Pam, who earned an 1800 on her SAT, or Jim, who scored a 24 on his ACT?





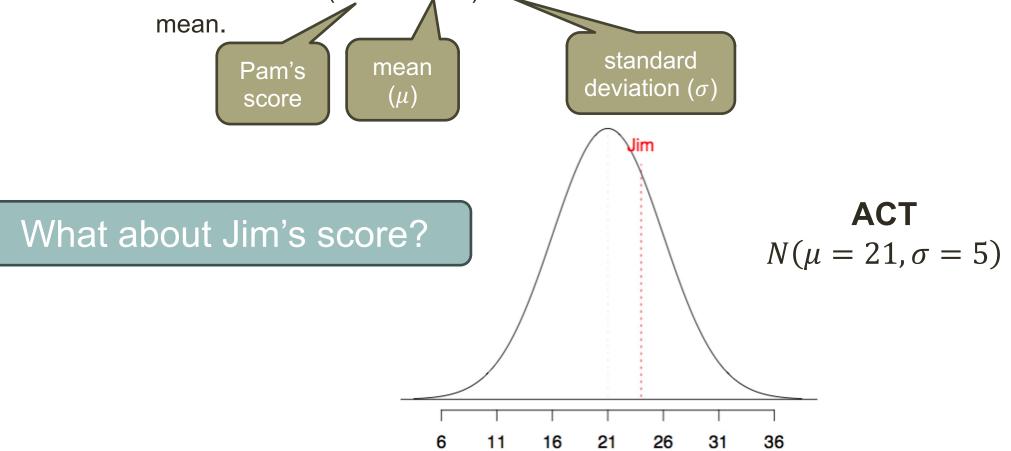
Since we cannot just compare these two raw scores, we instead compare how many standard deviations beyond the mean each observation is.

• Pam's score is (1800 - 1500) / 300 = 1 standard deviation above the

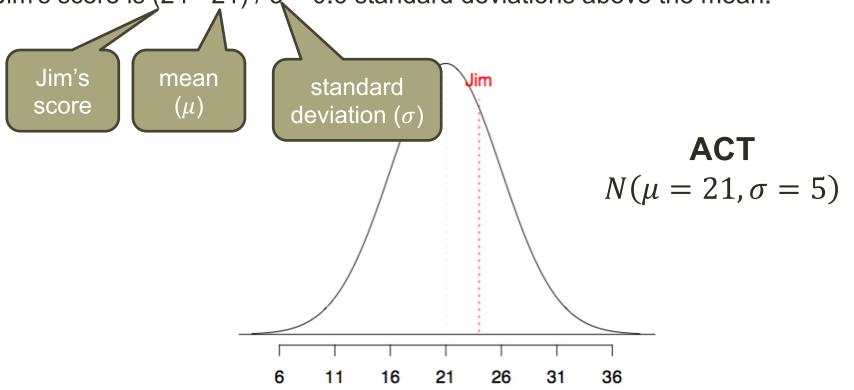


Since we cannot just compare these two raw scores, we instead compare how many standard deviations beyond the mean each observation is.

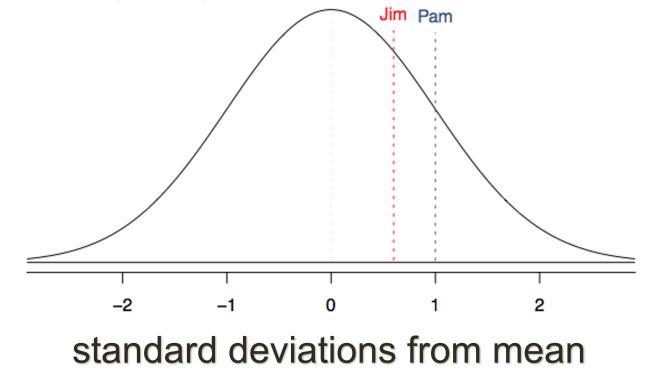
• Pam's score is (1800 - 1500) / 300 = 1 standard deviation above the



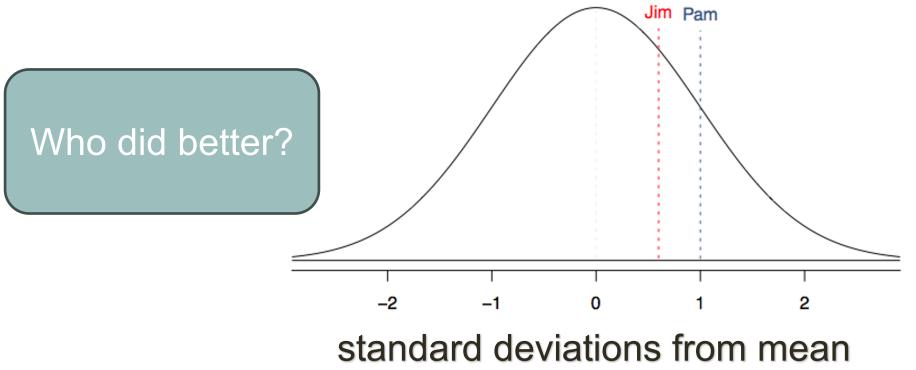
- Pam's score is (1800 1500) / 300 = 1 standard deviation above the mean.
- Jim's score is (24 21) / 5 = 0.6 standard deviations above the mean.



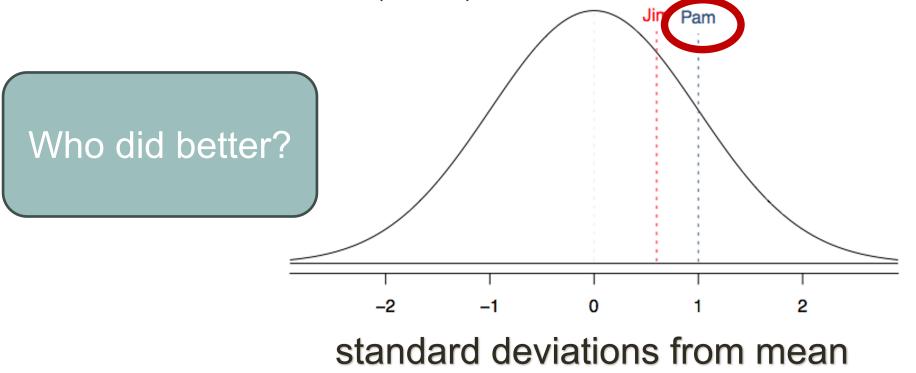
- Pam's score is (1800 1500) / 300 = 1 standard deviation above the mean.
- Jim's score is (24 21) / 5 = 0.6 standard deviations above the mean.



- Pam's score is (1800 1500) / 300 = 1 standard deviation above the mean.
- Jim's score is (24 21) / 5 = 0.6 standard deviations above the mean.



- Pam's score is (1800 1500) / 300 = 1 standard deviation above the mean.
- Jim's score is (24 21) / 5 = 0.6 standard deviations above the mean.



Standardizing with Z scores

These are called *standardized* scores, or *Z* scores.

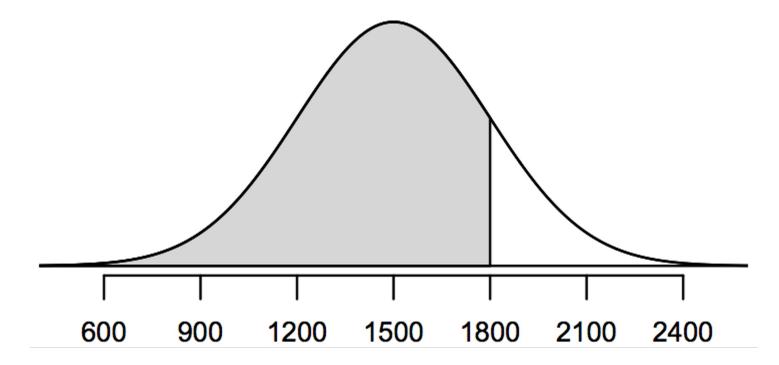
• Z score of an observation is the number of standard deviations it falls above or below the mean.

 $Z = \frac{observation - mean}{SD}$

- Z scores are defined for distributions of any shape, but only when the distribution is normal can we use Z scores to calculate percentiles (more on this next).
- Observations that are more than 2 SD away from the mean (|Z| > 2) are typically considered unusual.

Percentiles

- *Percentile* is the percentage of observations that fall below a given data point.
- Graphically, percentile is the area below the probability distribution curve to the left of that observation.



Calculating percentiles - using tables

[Second decimal place of Z										
Z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09		
0.0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359		
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753		
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141		
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517		
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879		
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224		
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549		
0.7	0.7580	Pam	's Z sco	ore ' ³	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852		
0.8	0.7881	V	/as 1.0	57	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133		
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389		
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621		
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8810	0.8830		
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015		

Calculating percentiles - using tables

				Seco	nd decin	cimal place of Z						
Z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09		
0.0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359		
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753		
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141		
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517		
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879		
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224		
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549		
0.7	0.7580	Pam	's Z sco	ore 3	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852		
0.8	0.7881	W	/as 1.0	57	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133		
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389		
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621		
1.1	0.8643	U.	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8810	0.8830		
1.2	0.8849	\int	84% of	F	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015		
		obse	ervation	s are								
		less	than P	am's								

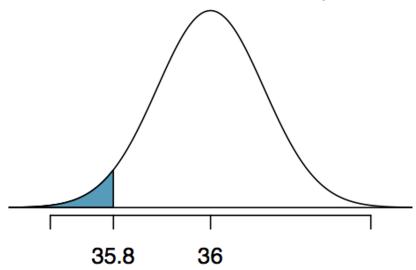


At Heinz ketchup factory the amounts which go into bottles of ketchup are supposed to be normally distributed with mean 36 oz. and standard deviation 0.11 oz. Once every 30 minutes a bottle is selected from the production line, and its contents are noted precisely. If the amount of ketchup in the bottle is below 35.8 oz. or above 36.2 oz., then the bottle fails the quality control inspection. What percent of bottles have less than 35.8 ounces of ketchup?

• Let X = amount of ketchup in a bottle: $X \sim N(\mu = 36, \sigma = 0.11)$

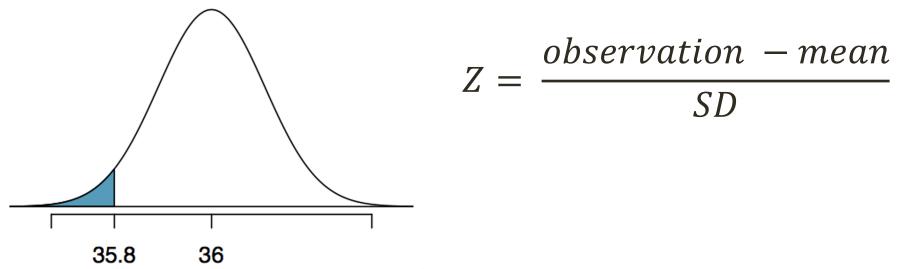
At Heinz ketchup factory the amounts which go into bottles of ketchup are supposed to be normally distributed with mean 36 oz. and standard deviation 0.11 oz. Once every 30 minutes a bottle is selected from the production line, and its contents are noted precisely. If the amount of ketchup in the bottle is below 35.8 oz. or above 36.2 oz., then the bottle fails the quality control inspection. What percent of bottles have less than 35.8 ounces of ketchup?

• Let X = amount of ketchup in a bottle: $X \sim N(\mu = 36, \sigma = 0.11)$



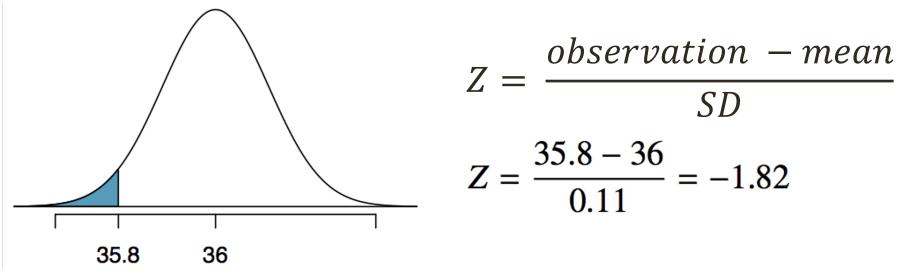
At Heinz ketchup factory the amounts which go into bottles of ketchup are supposed to be normally distributed with mean 36 oz. and standard deviation 0.11 oz. Once every 30 minutes a bottle is selected from the production line, and its contents are noted precisely. If the amount of ketchup in the bottle is below 35.8 oz. or above 36.2 oz., then the bottle fails the quality control inspection. What percent of bottles have less than 35.8 ounces of ketchup?





At Heinz ketchup factory the amounts which go into bottles of ketchup are supposed to be normally distributed with mean 36 oz. and standard deviation 0.11 oz. Once every 30 minutes a bottle is selected from the production line, and its contents are noted precisely. If the amount of ketchup in the bottle is below 35.8 oz. or above 36.2 oz., then the bottle fails the quality control inspection. What percent of bottles have less than 35.8 ounces of ketchup?





Т

Z	0	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09	chup are
-0	.50000	.49601	.49202	.48803	.48405	.48006	.47608	.47210	.46812	.46414	•
-0.1	.46017	.45620	.45224	.44828	.44433	.44034	.43640	.43251	.42858	.42465	ard deviation
-0.2	.42074	.41683	.41294	.40905	.40517	.40129	.39743	.39358	.38974	.38591	Juction line,
-0.3	.38209	.37828	.37448	.37070	.36693	.36317	.35942	.35569	.35197	.34827	· · · · · · · · · · · · · · · · · · ·
-0.4	.34458	.34090	.33724	.33360	.32997	.32636	.32276	.31918	.31561	.31207	he bottle is
-0.5	.30854	.30503	.30153	.29806	.29460	.29116	.28774	.28434	.28096	.27760	control
-0.6	.27425	.27093	.26763	.26435	.26109	.25785	.25463	.25143	.24825	.24510	
-0.7	.24196	.23885	.23576	.23270	.22965	.22663	.22363	.22065	.21770	.21476	f ketchup?
-0.8	.21186	.20897	.20611	.20327	.20045	.19766	.19489	.19215	.18943	.18673	()
-0.9	.18406	.18141	.17879	.17619	.17361	.17106	.16853	.16602	.16354	.16109	/
-1	.15866	.15625	.15386	.15151	.14917	.14686	.14457	.14231	.14007	.13786	
-1.1	.13567	.13350	.13136	.12924	.12714	.12507	.12302	.12100	.11900	.11702	ion – mean
-1.2	.11507	.11314	.11123	.10935	.10749	.10565	.10383	.10204	.10027	.09853	
-1.3	.09680	.09510	.09342	.09176	.09012	.08851	.08692	.08534	.08379	.08226	
-1.4	.08076	.07927	.07780	.07636	.07493	.07353	.07215	.07078	.06944	.06811	SD
-1.5	.06681	.06552	.06426	.06301	.06178	.06057	.05938	.05821	.05705	.05592	
-1.6	.05480	.05370	.05262	.05155	.05050	.04947	.04846	.04746	.04648	.04551	1.00
-1.7	.04457	.04363	.04272	.04182	.04093	.04006	.03920	.03836	.03754	.03673	-1.82
-1.8	.03593	.03515	.03438	.03362	.03288	.03216	.03144	.03074	.03005	.02938	
-1.5	.02072	.02807	.02743	.02660	.02619	.02559	.02500	.02442	.02385	.02330	
-2	.02275	.02222	.02169	.02118	.02068	.02018	.01970	.01923	.01876	.01831	
2.1	01796	01742	01700	01650	01610	01570	01520	01500	01462	01426	

https://www.ztable.net/#google_vignette

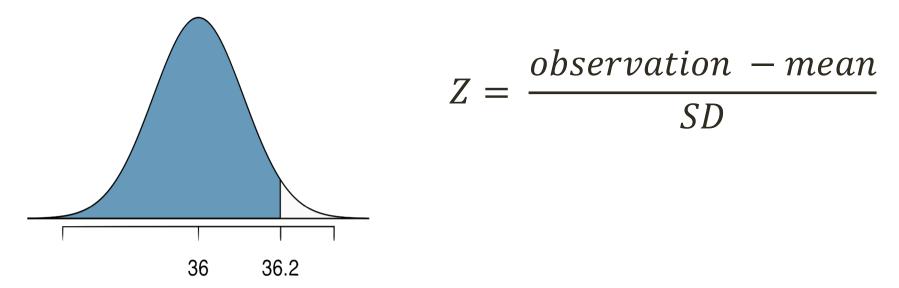


3.4% of bottles have less than 35.8 oz of ketchup



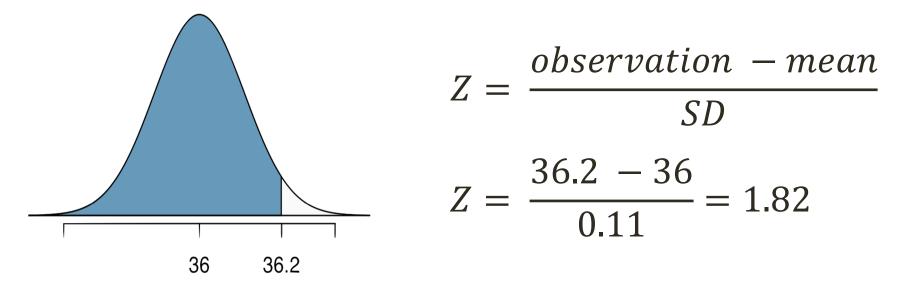
At Heinz ketchup factory the amounts which go into bottles of ketchup are supposed to be normally distributed with mean 36 oz. and standard deviation 0.11 oz. Once every 30 minutes a bottle is selected from the production line, and its contents are noted precisely. If the amount of ketchup in the bottle is below 35.8 oz. or above 36.2 oz., then the bottle fails the quality control inspection. What percent of bottles have more than 36.2 ounces of ketchup?

Let X = amount of ketchup in a bottle: $X \sim N(\mu = 36, \sigma = 0.11)$



At Heinz ketchup factory the amounts which go into bottles of ketchup are supposed to be normally distributed with mean 36 oz. and standard deviation 0.11 oz. Once every 30 minutes a bottle is selected from the production line, and its contents are noted precisely. If the amount of ketchup in the bottle is below 35.8 oz. or above 36.2 oz., then the bottle fails the quality control inspection. What percent of bottles have more than 36.2 ounces of ketchup?

Let X = amount of ketchup in a bottle: $X \sim N(\mu = 36, \sigma = 0.11)$



 Z	0	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09	
+0	.50000	.50399	.50798	.51197	.51595	.51994	.52392	.52790	.53188	.53586	
+0.1	.53983	.54380	.54776	.55172	.55567	.55966	.56360	.56749	.57142	.57535) are
+0.2	.57926	.58317	.58706	.59095	.59483	.59871	.60257	.60642	.61026	.61409	eviation
+0.3	.61791	.62172	.62552	.62930	.63307	.63683	.64058	.64431	.64803	.65173	on line,
 +0.4	.65542	.65910	.66276	.66640	.67003	.67364	.67724	.68082	.68439	.68793	,
+0.5	.69146	.69497	.69847	.70194	.70540	.70884	.71226	.71566	.71904	.72240	ottle is
 +0.6	.72575	.72907	.73237	.73565	.73891	.74215	.74537	.74857	.75175	.75490	ol
+0.7	.75804	.76115	.76424	.76730	.77035	.77337	.77637	.77935	.78230	.78524	of
 +0.8	.78814	.79103	.79389	.79673	.79955	.80234	.80511	.80785	.81057	.81327	·1
+0.9	.81594	.81859	.82121	.82381	.82639	.82894	.83147	.83398	.83646	.83891	
 +1	.84134	.84375	.84614	.84849	.85083	.85314	.85543	.85769	.85993	.86214	
+1.1	.86433	.86650	.86864	.87076	.87286	.87493	.87698	.87900	.88100	.88298	
 +1.2	.88493	.88686	.88877	.89065	.89251	.89435	.89617	.89796	.89973	.90147	
+1.3	.90320	.90490	.90658	.90824	.90988	.91149	.91308	.91466	.91621	.91774	moan
 +1.4	.91924	.92073	.92220	.92364	.92507	.92647	.92785	.92922	.93056	.93189	. — mean
+1.5	.93319	.93448	.93574	.93699	.93822	.93943	.94062	.94179	.94295	.94408	
 +1.6	.94520	.94630	.94738	.94845	.94950	.95053	.95154	.95254	.95352	.95449	
+1.7	.95543	.95637	.95728	.95818	.95907	.95994	.96080	.96164	.96246	.96327	
 +1.8	.96407	.96485	.96562	.96638	.96712	.96784	.96856	.96926	.96995	.97062	
+1.9	.97128	.97193	.97257	.97320	.97381	.97441	.97500	.97558	.97615	.97670	1.82
 +2	.97725	.97778	.97831	.97882	.97932	.97982	.98030	.98077	.98124	.98169	1.02
+7 1	98214	08257	08300	083/11	08387	98/177	98461	98500	08537	08574	

https://www.ztable.net/#google_vignette

Z	0	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09	_
+0	.50000	.50399	.50798	.51197	.51595	.51994	.52392	.52790	.53188	.53586	
+0.1	.53983	.54380	.54776	.55172	.55567	.55966	.56360	.56749	.57142	.57535) are
+0.2	.57926	.58317	.58706	.59095	.59483	.59871	.60257	.60642	.61026	.61409	eviation
+0.3	.61791	.62172	.62552	.62930	.63307	.63683	.64058	.64431	.64803	.65173	on line,
+0.4	.65542	.65910	.66276	.66640	.67003	.67364	.67724	.68082	.68439	.68793	,
+0.5	.69146	.69497	.69847	.70194	.70540	.70884	.71226	.71566	.71904	.72240	ottle is
+0.6	.72575	.72907	.73237	.73565	.73891	.74215	.74537	.74857	.75175	.75490	ol
+0.7	.75804	.76115	.76424	.76730	.77035	.77337	.77637	.77935	.78230	.78524	of
+0.8	.78814	.79103	.79389	.79673	.79955	.80234	.80511	.80785	.81057	.81327	· · ·
+0.9	.81594	.81859	.82121	.82381	.82639	.82894	.83147	.83398	.83646	.83891	
+1	.84134	.84375	.84614	.84849	.85083	.85314	.85543	.85769	.85993	.86214	
+1.1	.86433	.86650	.86864	.87076	.87286	.87493	.87698	.87900	.88100	.88298	
+1.2	.88493	.88686	.88877	.89065	.89251	.89435	.89617	.89796	.89973	.90147	
+1.3	.90320	.90490	.90658	.90824	.90988	.91149	.91308	.91466	.91621	.91774	moan
+1.4	.91924	.92073	.92220	.92364	.92507	.92647	.92785	.92922	.93056	.93189	. — mean
+1.5	.93319	.93448	.93574	.93699	.93822	.93943	.94062	.94179	.94295	.94408	
+1.6	.94520	.94630	.94738	.94845	.94950	.95053	.95154	.95254	.95352	.95449	
+1.7	.95543	.95637	.95728	.95818	.95907	.95994	.96080	.96164	.96246	.96327	
+1.8	.96407	.96485	.96562	.96638	.96712	.96784	.96856	.96926	.96995	.97062	
+1.9	.97128	.97193	.97257	.97320	.97381	.97441	.97500	.97558	.97615	.97670	1.82
+2	.97725	.97778	.97831	.97882	.97932	.97982	.98030	.98077	.98124	.98169	1.02
+2.1	98214	08257	08300	083/11	08383	98422	98461	98500	08537	98574	

https://www.ztable.net/#google_vignette



96.6% of bottles have less than 36.2 oz of ketchup

??% of bottles have more than 36.2 oz of ketchup

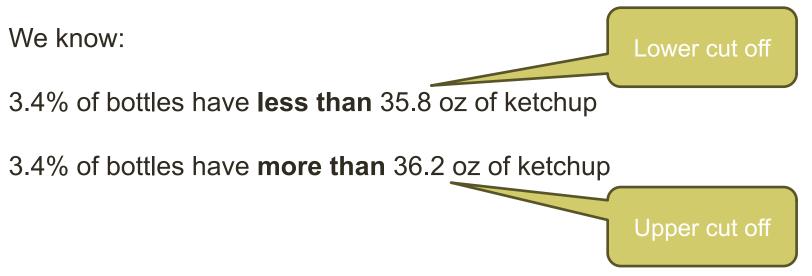


96.6% of bottles have less than 36.2 oz of ketchup

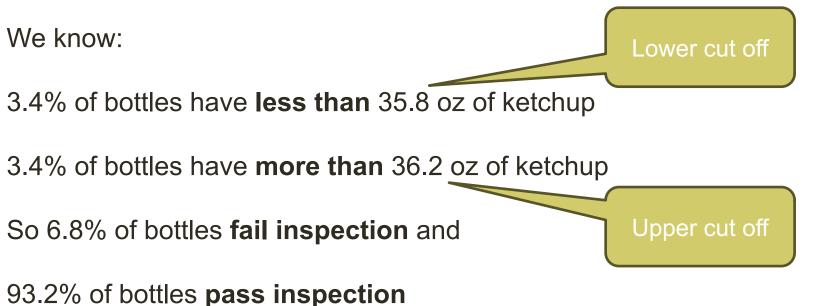
3.4% of bottles have more than 36.2 oz of ketchup













We know:

3.4% of bottles have less than 35.8 oz of ketchup

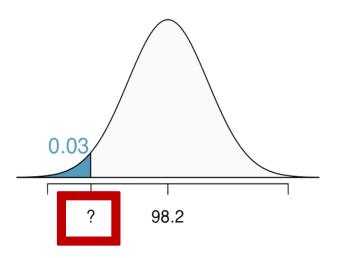
3.4% of bottles have more than 36.2 oz of ketchup

So 6.8% of bottles fail inspection and

93.2% of bottles pass inspection

Body temperatures of healthy humans are distributed nearly normally with mean 98.2°F and standard deviation 0.73°F. What is the cutoff for the lowest 3% of human body temperatures?

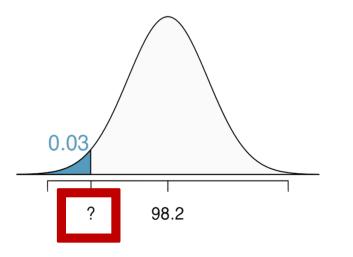
Body temperatures of healthy humans are distributed nearly normally with mean 98.2°F and standard deviation 0.73°F. What is the cutoff for the lowest 3% of human body temperatures?



Z	0	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09	
-0	.50000	.49601	.49202	.48803	.48405	.48006	.47608	.47210	.46812	.46414	
-0.1	.46017	.45620	.45224	.44828	.44433	.44034	.43640	.43251	.42858	.42465	
-0.2	.42074	.41683	.41294	.40905	.40517	.40129	.39743	.39358	.38974	.38591	
-0.3	.38209	.37828	.37448	.37070	.36693	.36317	.35942	.35569	.35197	.34827	
-0.4	.34458	.34090	.33724	.33360	.32997	.32636	.32276	.31918	.31561	.31207	
-0.5	.30854	.30503	.30153	.29806	.29460	.29116	.28774	.28434	.28096	.27760	
-0.6	.27425	.27093	.26763	.26435	.26109	.25785	.25463	.25143	.24825	.24510	
-0.7	.24196	.23885	.23576	.23270	.22965	.22663	.22363	.22065	.21770	.21476	
-0.8	.21186	.20897	.20611	.20327	.20045	.19766	.19489	.19215	.18943	.18673	าds to
-0.9	.18406	.18141	.17879	.17619	.17361	.17106	.16853	.16602	.16354	.16109	105 10
-1	.15866	.15625	.15386	.15151	.14917	.14686	.14457	.14231	.14007	.13786	
-1.1	.13567	.13350	.13136	.12924	.12714	.12507	.12302	.12100	.11900	.11702	
-1.2	.11507	.11314	.11123	.10935	.10749	.10565	.10383	.10204	.10027	.09853	
-1.3	.09680	.09510	.09342	.09176	.09012	.08851	.08692	.08534	.08379	.08226	
-1.4	.08076	.07927	.07780	.07636	.07493	.07353	.07215	.07078	.06944	.06811	
-1.5	.06681	.06552	.06426	.06301	.06178	.06057	.05938	.05821	.05705	.05592	
-1.6	.05480	.05370	.05262	.05155	.05050	.04947	.04846	.04746	.04648	.04551	
-1.7	.04457	.04363	.04272	.04182	.04093	.04006	.03920	.03836	03754	.03673	
-1.8	.03593	.03515	.03438	.03362	.03288	.03216	.03144	.03074	.03005	.02938	
-1.9	.02872	.02807	.02743	.02680	.02619	.02559	.02500	.02442	.02385	.02330	
-2	.02275	.02222	.02169	.02118	.02068	.02018	.01970	.01923	.01876	.01831	
-2.1	.01786	.01743	.01700	.01659	.01618	.01578	.01539	.01500	.01463	.01426	
-2.2	.01390	.01355	.01321	.01287	.01255	.01222	.01191	.01160	.01130	.01101	
.23	01072	01044	01017	00000	00964	00030	00014	00880	00866	00842	

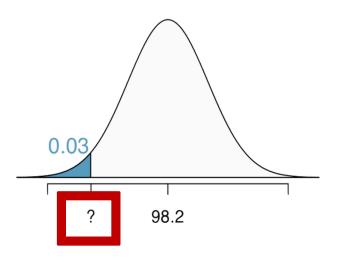
Z	0	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09	-
-0	.50000	.49601	.49202	.48803	.48405	.48006	.47608	.47210	.46812	.46414	
-0.1	.46017	.45620	.45224	.44828	.44433	.44034	.43640	.43251	.42 <mark>858</mark>	.42465	
-0.2	.42074	.41683	.41294	.40905	.40517	.40129	.39743	.39358	.38 <mark>9</mark> 74	.38591	
-0.3	.38209	.37828	.37448	.37070	.36693	.36317	.35942	.35569	.35 <mark>197</mark>	.34827	
-0.4	.34458	.34090	.33724	.33360	.32997	.32636	.32276	.31918	.31561	.31207	
-0.5	.30854	.30503	.30153	.29806	.29460	.29116	.28774	.28434	.28096	.27760	
-0.6	.27425	.27093	.26763	.26435	.26109	.25785	.25463	.25143	.24 <mark>825</mark>	.24510	
-0.7	.24196	.23885	.23576	.23270	.22965	.22663	.22363	.22065	.21 <mark>770</mark>	.21476	
-0.8	.21186	.20897	.20611	.20327	.20045	.19766	.19489	.19215	.18943	.18673	nds to 0
-0.9	.18406	.18141	.17879	.17619	.17361	.17106	.16853	.16602	.16 <mark>854</mark>	.16109	105 10 0
-1	.15866	.15625	.15386	.15151	.14917	.14686	.14457	.14231	.14007	.13786	
-1.1	.13567	.13350	.13136	.12924	.12714	.12507	.12302	.12100	.11 <mark>900</mark>	.11702	
-1.2	.11507	.11314	.11123	.10935	.10749	.10565	.10383	.10204	.10027	.09853	
-1.3	.09680	.09510	.09342	.09176	.09012	.08851	.08692	.08534	.08 <mark>879</mark>	.08226	
-1.4	.08076	.07927	.07780	.07636	.07493	.07353	.07215	.07078	.06 <mark>944</mark>	.06811	
-1.5	.06681	.06552	.06426	.06301	.06178	.06057	.05938	.05821	.05705	.05592	
-1.6	.05480	.05370	.05262	.05155	.05050	.04947	.04846	.04746	.04548	.04551	
-1.7	.04457	.04363	.04272	.04182	.04093	.04006	.03920	.03836	.03754	.03673	Z = -1.
-1.8		.00010	.00400	.00002	.05200	.00210		.05074	.03005	.02938	~ '.
-1.9	.02872	.02807	.02743	.02680	.02619	.02559	.02500	.02442	.02385	.02330	
-2	.02275	.02222	.02169	.02118	.02068	.02018	.01970	.01923	.01876	.01831	
-2.1	.01786	.01743	.01700	.01659	.01618	.01578	.01539	.01500	.01463	.01426	
-2.2	.01390	.01355	.01321	.01287	.01255	.01222	.01191	.01160	.01130	.01101	
.23	01072	01044	01017	00000	00964	00030	00014	008800	00866	00842	

Body temperatures of healthy humans are distributed nearly normally with mean 98.2°F and standard deviation 0.73°F. What is the cutoff for the lowest 3% of human body temperatures?



First, we need the Z score that corresponds to 0.03Z = -1.88

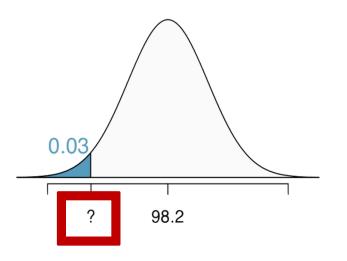
Body temperatures of healthy humans are distributed nearly normally with mean 98.2°F and standard deviation 0.73°F. What is the cutoff for the lowest 3% of human body temperatures?



First, we need the Z score that corresponds to 0.03Z = -1.88

Now, we solve for the observation that would give us this Z

Body temperatures of healthy humans are distributed nearly normally with mean 98.2°F and standard deviation 0.73°F. What is the cutoff for the lowest 3% of human body temperatures?

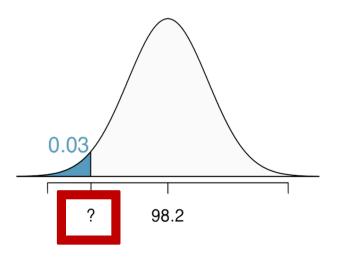


First, we need the Z score that corresponds to 0.03Z = -1.88

Now, we solve for the observation that would give us this Z:

$$Z = \frac{observation - mean}{SD}$$
$$-1.88 = \frac{x - 98.2}{0.73}$$

Body temperatures of healthy humans are distributed nearly normally with mean 98.2°F and standard deviation 0.73°F. What is the cutoff for the lowest 3% of human body temperatures?

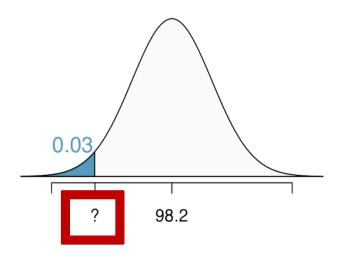


First, we need the Z score that corresponds to 0.03Z = -1.88

Now, we solve for the observation that would give us this Z:

$$Z = \frac{observation - mean}{SD}$$
$$-1.88 = \frac{x - 98.2}{0.73}$$
$$x = 96.8$$

Body temperatures of healthy humans are distributed nearly normally with mean 98.2°F and standard deviation 0.73°F. What is the cutoff for the lowest 3% of human body temperatures?



First, we need the Z score that corresponds to 0.03Z = -1.88

Now, we solve for the observation that would give us this Z:

96.8 degrees F is the cut off for the lowest 3% of human body temperatures.

$$Z = \frac{observation - mean}{SD}$$
$$-1.88 = \frac{x - 98.2}{0.73}$$
$$x = 96.8$$

Body temperatures of healthy humans are distributed nearly normally with mean 98.2°F and standard deviation 0.73°F. What is the cutoff for the highest 10% of human body temperatures?

(a) 97.3°F	(c) 99.4°F
(b) 99.1°F	(d) 99.6°F

First, we need the Z score that corresponds to 90% Z = ??

Then, solve for the observation that would give us this Z:

$$Z = \frac{observation - mean}{SD}$$

Body temperatures of healthy humans are distributed nearly normally with mean 98.2°F and standard deviation 0.73°F. What is the cutoff for the highest 10% of human body temperatures?

(a) 97.3°F	(c) 99.4°F
(b) 99.1°F	(d) 99.6°F

First, we need the Z score that corresponds to 90%Z = ??

Then, solve for the observation that would give us this Z:

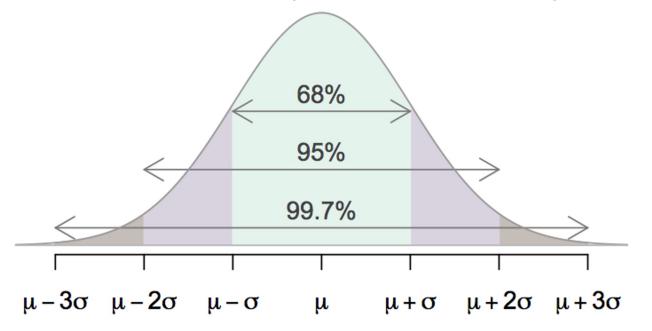
$$Z = \frac{observation - mean}{SD}$$

68-95-99.7 Rule

For nearly normally distributed data,

- about 68% falls within 1 SD of the mean,
- about 95% falls within 2 SD of the mean,
- about 99.7% falls within 3 SD of the mean.

It is possible for observations to fall 4, 5, or more standard deviations away from the mean, but these occurrences are very rare if the data are nearly normal.



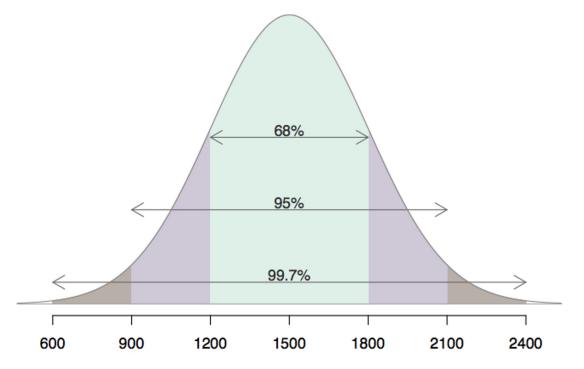
Describing variability using the 68-95-99.7 Rule

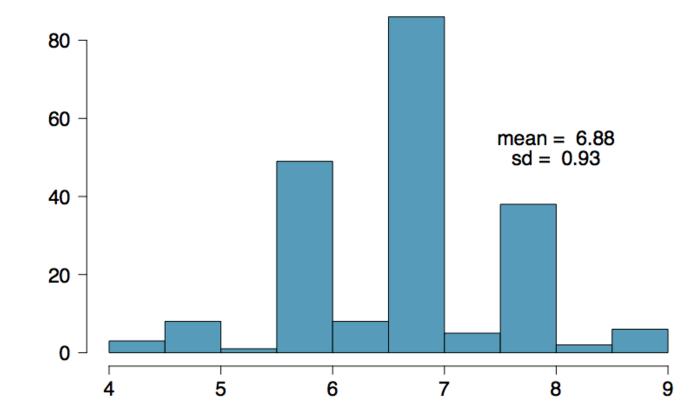
SAT scores are distributed nearly normally with mean 1500 and standard deviation 300.

Describing variability using the 68-95-99.7 Rule

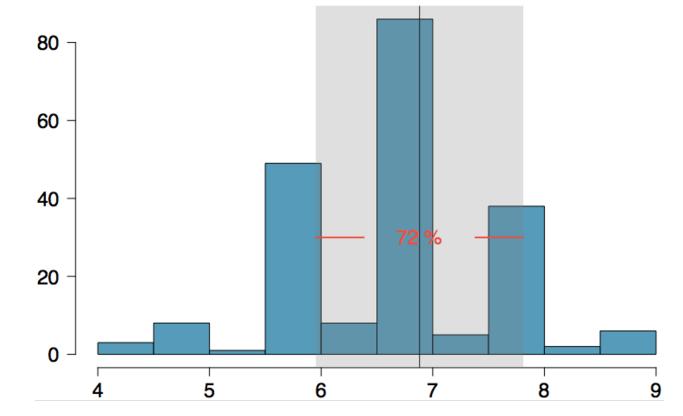
SAT scores are distributed nearly normally with mean 1500 and standard deviation 300.

- ~68% of students score between 1200 and 1800 on the SAT.
- ~95% of students score between 900 and 2100 on the SAT.
- ~\$99.7% of students score between 600 and 2400 on the SAT.

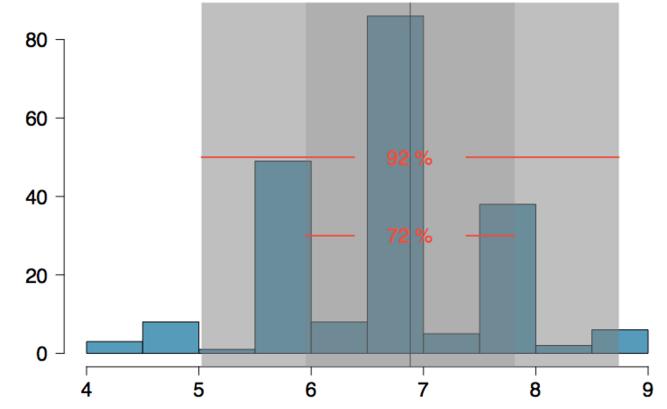




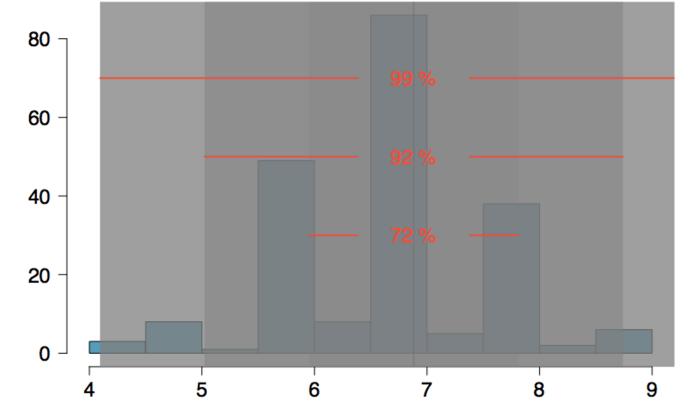
• Mean = 6.88 hours, SD = 0.92 hrs



- Mean = 6.88 hours, SD = 0.92 hrs
- 72% of the data are within 1 SD of the mean: 6.88 ± 0.93



- Mean = 6.88 hours, SD = 0.92 hrs
- 72% of the data are within 1 SD of the mean: 6.88 ± 0.93
- 92% of the data are within 1 SD of the mean: 6.88 ± 2 x 0.93



- Mean = 6.88 hours, SD = 0.92 hrs
- 72% of the data are within 1 SD of the mean: 6.88 ± 0.93
- 92% of the data are within 1 SD of the mean: 6.88 ± 2 x 0.93
- 99% of the data are within 1 SD of the mean: 6.88 ± 3 x 0.93

Which of the following is <u>false</u>?

- A. Majority of Z scores in a right skewed distribution are negative.
- B. In skewed distributions the Z score of the mean might be different than 0.
- C. For a normal distribution, IQR is less than 2 x SD.
- D. Z scores are helpful for determining how unusual a data point is compared to the rest of the data in the distribution.

Which of the following is <u>false</u>?

- A. Majority of Z scores in a right skewed distribution are negative.
- B. In skewed distributions the Z score of the mean might be different than 0.
- C. For a normal distribution, IQR is less than 2 x SD.
- D. Z scores are helpful for determining how unusual a data point is compared to the rest of the data in the distribution.